

Balancer

Security assessment by HashEye · prepared for Balancer

HASHEYE AUDITED

PROJECT	Balancer
CLIENT	Balancer
CATEGORY	Blockchain
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This report was produced under HashEye's layered review process – **automated detection**, **pattern correlation**, and **senior manual verification** – with every finding signed off by a human reviewer. Full findings detail and on-chain attestation are available on the report page at hashey.io/audits/research-balancer-2020-01-01-h74863.

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ExecutiveSummary ProjectDashboard CodeMaturityEvaluation EngagementGoals Coverage
AutomatedTestingandVerification AutomatedTestingwithEchidna StableMathArithmeticProperties
WeightedMathArithmeticProperties AutomatedTestingwithSlither RecommendationsSummary ShortTerm
LongTerm FindingsSummary 1.Maliciousmanagercanreinvesttokenstodrainthepool
2.Transfer tozerocanleadtounexpectedburns 3.Soliditycompileroptimizationscanbedangerous
4.Missingeventsforcriticaloperations 5.Lackofzerocheckonfunctions
10.LackofrobustsafeguardsforpoolswithanemptytokeninWeightedPool 11.Protocolfeefront-run
12.Sumofnormalizedweightscanbedifferentfrom1
14.Emergencyperiodtogglingcanbeusedtoselectivelyblocktransactions
6.StableMath._calcOutGivenInmayallowfreeswaps 7.StableMath._calcInGivenOutmayallowfreeswaps
8.StableMath._calcTokenInGivenExactBptOutmayallowanattacker tojoinforfree
9.BalancerStablePool'sinvariantcandiffersignificantlyfromCurve'sinvariant
13.StablePool'sinvariantisnotmonotonicallyincreasing A.VulnerabilityClassifications
B.CodeMaturityClassifications C.CodeQualityRecommendations PoolRegistry BasePool BasePoolFactory
2021hasheyBalancerV2Assessment|1

StablePoolUserDataHelpers WeightedPoolUserDataHelpers CodeSizeOptimizations
D.TokenIntegrationChecklist GeneralSecurityConsiderations ERCConformity ContractComposition
Ownerprivileges TokenScarcity E.RisksAssociatedwithArbitraryPools
F.CheckingnonReentrantModifierswithSlither G.DifferentialFuzzingonBalancer<Curve H.Fixed-
PointRoundingRecommendations RoundingPrimitives Fixed-PointPrimitives
DeterminingtheRoundingDirection PowerRounding (1-x)vs.(x-1)Rounding RoundingResults joinPool
exitPool _tokenInForExactBPTOut _bptInForExactTokensOut _inGivenOut _outGivenIn
2021hasheyBalancerV2Assessment|2

ExecutiveSummary FromMarch22toApril2,2021,Balancerengagedhasheyetoreviewtheseecurityof
BalancerV2.hasheyconductedthisassessmentoverfourperson-weeks,withtwo engineersworkingfromcommits
2c84113 and bce652f fromthebalancer-core-v2 repository.
hasheyperformedapreviousauditofthisprojectoversixperson-weeksinJanuary
2021.Duringthataudit,17issueswerefound,includng7relatedtorounding. AppendixH
containsourroundingrecommendationsresultingfromthisinitialaudit.
Inthefirstweekofthisaudit,wefocusedonunderstandingthecodebase,includngthe
components'interactions witheachother,andlookedforthemostcommonSolidity
securityflaws.Weconcentratedonthevault.Inthesecondweek,wefocusedonthe pool
contractsandfeessystem.WealsousedEchidnatocheckforroundingerrorsinthemath
contractsusedbythepools,withafocusonthestablepool. Wefound14issues.Oneofthehigh-severityissues(TOB-
BALANCER-001)couldallowan assetmanagertodrainapoolofallofthetokensnotunderhisorhermanagement.We
alsofoundmanyarithmeticissuesinthestablepool,includngsomethatcouldleadto tokendraining.
Inadditiontothesecurityfindings,weidentifiedcodequalityissuesnotrelatedtoany
particularvulnerability,whicharediscussedinAppendixC.AppendixDcontains
recommendationsonevaluatingarbitraryERC20tokens,andAppendixEprovides
recommendationsonarbitrarypools.AppendixFcontainsascriptbuiltinontopofSlitherto reviewthecontracts'
nonReentrant modifiers.AnEchidna-baseddifferentialfuzzerofthe
CurveandBalancerstablepoolarithmeticisprovidedinAppendixG.
Overall,theBalancerV2projectfollowsbestpractices.Thecode'sstructurehasbeen
improvedsinceouroriginalaudit,andBalancerhasavoidedthemainSoliditypitfalls.
However,the code'sunderlyingcomplexityandseveral movingparts increasethelike-
likelihoodofmistakes.Balancerimplementedourroundingrecommendationsforthe WeightedPool
,buttheroundingissuesfoundinthe StablePool indicatethatthecode's
arithmetic hasroomforimprovementandthatmoreissuesmightbepresent.Finally,at
thetimeoftheaudit,thecodewasunstableandundergoingchanges,includngsomethat
werenotreviewedinthisaudit. hasheyerecommends thatBalancertakethefollowingsteps: •
Addressallreportedissues. • ImplementadditionalEchidnateststovalidatetheroundingofallarithmetic.
2021hasheyBalancerV2Assessment|3

- Documentthedangersofusingnon-standardERC20tokens(e.g.,deflationary tokens),and,usingAppendixD,developanERC20tokenchecklistforusers. •

Document the pools' assumptions and develop a check list for arbitrary pools based on Appendix E. •
Perform an audit on the code base as it has stabilized. 2021 hashey Balancer V2 Assessment | 4

Project Dashboard Application Summary Name Balancer V2 Version 2c84113 , bce652f Type Solidity
Platform Ethereum Engagement Summary Dates March 22 - April 2, 2021 Method Whitebox Consultants Engaged 2
Level of Effort 4 person-weeks Vulnerability Summary Total High-Severity Issues 2 Total Medium-
Severity Issues 3 Total Low-Severity Issues 5 Total Informational-Severity Issues 3
Total Undetermined-Severity Issues 1 Total 14 Category Breakdown Access Controls 1 Auditing and Logging 1
Data Validation 8 Undefined Behavior 4 Total 14 2021 hashey Balancer V2 Assessment | 5

Code Maturity Evaluation Category Name Description

Access Controls Satisfactory. The project uses a robust authentication and authorization system.

Arithmetic Moderate. Many issues stem from a lack of proper rounding

validation, and more of those issues might be present. The code base would benefit from case-by-
case handling of the rounding direction.

Assembly Use Moderate. While the use of assembly is limited and does not lead to
any security issues, it could be reduced by sharing structures across contracts.

Centralization Weak. There are limits on privileged users' actions. However, an
asset manager could easily abuse his or her privilege to drain a pool of all other assets (TOB-BALANCER-
001). Additionally, an admin could toggle the emergency period between active and inactive to
selectively block transactions (TOB-BALANCER-014).

Code Stability Weak. The code was undergoing significant changes during the
audit and will likely continue to evolve before reaching its final version.

Upgradeability Not Applicable. The system cannot be upgraded. Function Composition

Satisfactory. The overall code is well structured, and most of the

functions are small and have clear purposes. The critical functions can be easily extracted for testing. Front-

Running Moderate. Most functions contain arguments with limits to prevent
sudden changes that could negatively impact users' expectations

and ability to execute transactions as intended. However, a privileged user could front-
run withdrawal to quickly update the withdrawal fee (TOB-BALANCER-011).

Monitoring Satisfactory. Most functions emit events. However, one function for

changing the swap fee does not (TOB-BALANCER-004). Additionally,

the emission of a transfer event upon token burning could confuse users monitoring the events of the system (TOB-
BALANCER-002). Specification Moderate. The constant product arithmetic is well documented on

<https://balancer.finance/>. However, the overall system would benefit

from cleaner documentation on this architecture and assumption. 2021 hashey Balancer V2 Assessment | 6

Revising the documentation on fees and the components' interactions would also improve code readability.

Testing & Verification Moderate. The system has suitable unit tests but would benefit

from the addition of fuzzing or formal methods to ensure that the

arithmetic meets expectations. Many issues in this report were found using Echidna.

2021 hashey Balancer V2 Assessment | 7

Engagement Goals The engagement was scoped to provide a security assessment of the Balancer V2 smart contracts.

Specifically, we sought to answer the following questions: • Is it possible to cause a DoS in a pool? •

Is it possible for an asset manager or admin to abuse their abilities? •

Is it possible for pools to access funds belonging to other pools? •

Is the use of native and wrapped ETH implemented correctly? •

Do the arithmetic libraries correctly apply rounding? • Are fees applied correctly? •

Can swaps be used to steal funds? • Is the flash loan feature implemented correctly? •

Can the authentication/authorization scheme be circumvented? •

Is the internal balance accounting system working as expected? 2021 hashey Balancer V2 Assessment | 8

Coverage Authorizer + Authentication. Two small contracts that provide authorization and

authentication features throughout the contracts. We manually reviewed the

implementation to look for flaws that could allow an attacker to subvert the

authentication/authorization features.

Emergency Period. Implements an emergency period used in all of the pools and the vault.

We manually reviewed the implementation to look for flaws that could allow the admin to

turn the emergency period on and off at will.

Asset Transfer Handler. Contains functions for sending and receiving ERC20 tokens and

native/wrapped ETH. We manually reviewed the implementation for flaws related to

wrapping/unwrapping ETH and sending/receiving ERC20 tokens. Flash Loan Provider. Contains a single flashLoan

function. We reviewed the implementation to identify any flaws that could enable an attacker to borrow tokens
without repaying the flash loan.

Internal Balance. Stores the internal balance of each account as well as various helper

functions to add to or withdraw from the internal balance. We reviewed the balance update

functionstodiscernwhetheranattackercouldusetheaddressofanotherusers' funds. Wealsocheckedwhetherfeeswerecorrectlyappliedtothebalance. PoolRegistry. Contains thefunctionstoregister, join, or exit a pool and to register/deregister tokens of a pool, as well as helper functions to pack/unpack pool variables into/from a single bytes32 variable. We reviewed the implementation of the pack/unpack functions. We also reviewed all pool configuration-related functions to find flaws that would enable a pool to access or overwrite another pool's data or to otherwise disturb the internal accounting of pool registrations. Additionally, we reviewed the application of the fees for joining and exiting a pool. ProtocolFeesCollector, Fees. Contains functions to set global fee percentages and receives the collected fees, which can be withdrawn by the system admin. We manually checked that all functions correctly validated the input arguments and that the fee withdrawal process did not contain flaws. Swaps. Contains the main functions to initiate swaps, including multiple swaps in one call. We checked that the (chained) swaps did not contain flaws that could allow an attacker to steal funds. We checked that the correct pool specialization functions were called in all places. 2021hasheyBalancerV2Assessment|9

VaultAuthorization. Provides authorization helper functions and functions to set a relay on behalf of an account. We checked that the authorization functions did not contain flaws and that relayers were used correctly. Vault. Acts as the entry-point contract for Balancer and is where tokens are stored, user balances are updated, pools are registered, and flash loans are provided. We looked for flaws that could allow a malicious asset manager to steal assets. We checked the registration of pools, their tokens, and the addition and removal of liquidity for all three pool specialization types. We reviewed the use of native ETH and the conversion to wrapped ETH for flaws that could enable ETH theft. We reviewed the use of internal balances, including whether they could be used to steal tokens from the system. Additionally, we examined the storage of the packed balances in bytes32 and the various extraction functions. Pools (stable, weighted). We reviewed the pools' components, with a focus on their arithmetic and access controls. We confirmed that only the vault could call the join/exit operations. Using Echidna, we tested stable and weighted math and looked for flaws that could allow an attacker to gain tokens from swapping, joining, or exiting. Due to the time constraints, and because our original audit focused on the weighted pool, we concentrated our efforts on the stable pool arithmetic. Due to the number of stable pool arithmetic findings, we believe that more issues might be present. Due to the time constraints, hashey could not explore the following areas: • BalancerHelpers.sol • EnumerableMap.sol • LogExpMath.sol and its impact on callers 2021hasheyBalancerV2Assessment|10

Automated Testing and Verification

hashey used automated testing techniques to enhance coverage of certain areas of the contracts, including: • Slither, a Solidity static analysis framework. •

Echidna, a smart contract fuzzer. Echidna can rapidly test security properties via malicious, coverage-guided test case generation.

Automated testing techniques augment our manual security review but do not replace it.

Each method has limitations: Slither may identify security properties that fail to hold when

Solidity is compiled to EVM bytecode; Echidna may not randomly generate an edge case that violates a property.

Automated Testing with Echidna We implemented the following Echidna properties:

StableMathArithmeticProperties IDPropertyResult 1 StableMath._calcOutGivenIn cannot lead to free tokens. FAILED (TOB-BALAN CER-006) 2 StableMath._calcOutGivenIn cannot lead to free tokens with large balances. PASSED 3 StableMath._calcInGivenOut cannot lead to free tokens. FAILED (TOB-BALAN CER-007) 4 StableMath._calcInGivenOut cannot lead to free tokens with large balances. PASSED 5 StableMath._calcTokenInGivenExactBptOut cannot lead to free BPT tokens. FAILED (TOB-BALAN CER-008) 6 StableMath._calculateInvariant is monotonically increasing. FAILED (TOB-BALAN CER-014) 2021hasheyBalancerV2Assessment|11

7 StableMath._calculateInvariant does not differ significantly from Curve's invariant. FAILED (TOB-BALAN CER-009) 8 WeightedMathArithmeticProperties IDPropertyResult 8 WeightedMath._calcOutGivenIn cannot lead to free tokens. PASSED 9 WeightedMath._calcOutGivenIn cannot lead to free tokens with large balances. PASSED 10 WeightedMath._calcInGivenOut cannot lead to free tokens. PASSED 11 WeightedMath._calcTokenInGivenExactBptOut cannot lead to free BPT tokens. PASSED 12 WeightedMath._calculateInvariant is monotonically increasing. PASSED 13 The sum of all normalized weights in a pool is 1. FAILED (TOB-BALAN CER-012)

All the properties were run with pools containing four tokens, and with a test limit of five million.

Automated Testing with Slither We implemented the following Slither property: PropertyResult All Vault

RecommendationsSummary Thissectionaggregatesalltherecommendationsmadeduringtheengagement.Short-term recommendationsaddresstheimmediatecausesofissues.Long-termrecommendations pertaintothedevelopmentprocessandlong-termdesigngoals. ShortTerm
Documentthefactthatthemanagerhasaccesstoallofthefundsinthepool,or allowonemanagerperpool,insteadofonemanagerpertoken.Thiswillpreventuser confusionandreduce therisksassociatedwithmaliciousmanagers.TOB-BALANCER-001 Createa Burn eventorpreventtransfertothezeroaddress.Thiswillensurethatan attackercannotconfuseeventmonitorswithincorrectburnevents.TOB-BALANCER-002 Measurethegassavingsfromoptimizations,andcarefullyweighthemagainstthe possibilityofanoptimization-relatedbug.Thecompileroptimizerwasfrequentlythe sourceofbugsandshouldbecarefullyreviewed.TOB-BALANCER-003 Addeventsfor BasePool.setSwapFee , Authorizer.changeAuthorizer ,and Authorizer.changeRelayerAllowance .Eventswillfacilitatecontractmonitoringandthe detectionofsuspiciousbehavior.TOB-BALANCER-004 Addzero-valuechecksonallfunctionarguments.Thiswillensurethatuserscan't accidentallysetincorrectvalues,misconfiguringthesystem.TOB-BALANCER-005 Remove FixedPoint.mul and FixedPoint.div ,andensurethateveryfunctionuses theappropriateroundingdirection.Thesefunctionsareerror-proneandcanleadto roundingissues.TOB-BALANCER-006,TOB-BALANCER-007,TOB-BALANCER-008 Createtwoversionsof _calculateInvariant and _getTokenBalanceGivenInvariantAndAllOtherBalances thatroundupordown, respectively,andusethemappropriately.Severalissueswerecausedbyincorrect roundingstrategiesinthesetwofunctions.TOB-BALANCER-006,TOB-BALANCER-007, TOB-BALANCER-008 InvestigatethedifferencesbetweentheBalancerandCurveinvariants,and evaluatetheirimpactonarbitrageopportunitiesandpotentialassociatedrisks.The impactsoftheirdifferencesareunclearandshouldbereviewed.TOB-BALANCER-009 Disallowswap/join/exitoperationsifthebalanceofthetokenin hasbeen emptied,oriftheoperationswouldemptythetokenout .Theweightedpool'smethod

2021hasheyeBalancerV2Assessment|13

ofhandlingapoolwithanemptybalanceisfragile,andtheexistingmitigationscouldcease toworkifthecodeisrefactored.TOB-BALANCER-010 Addaminimumwithdrawalrequirementforwithdrawaloperations.Otherwise,a maliciousownercouldfront-runthewithdrawaloperationsandmakeuserspay higher-than-expectedfees.TOB-BALANCER-011 Checkthatthesumofthenormalizedweightsisequalto10**18intheweighted pool'sconstructor.Thiswillensurethatthepool'sinvariantispreservedatdeployment. TOB-BALANCER-012 Applythecorrectroundingin StableMath._calculateInvariant .Thecurrent invariantisnotmonotonicallyincreasing,whichcouldleadtounexpectedbehaviorinallof thestablepool'sformulas.TOB-BALANCER-013 Documenttheemergencyperiod-relatedabilitiesofanadminsothatuserswillbe wellinformed.TOB-BALANCER-014

2021hasheyeBalancerV2Assessment|14

LongTerm Documenttheexpectationsformanagersandtheirassociatedrisks.Consider providing smartcontractsthatcanactasmanagerswithon-chainrestrictions. TOB-BALANCER-001 Documentandtesttheexpectedbehaviorofallofthesystem'sevents.Consider usingablockchain-monitoringsystemtotrackanysuspiciousbehaviorinthecontracts. TOB-BALANCER-002 MonitorthedevelopmentandadoptionofSoliditycompileroptimizationsto assesstheirmaturity.Thedeploymentrequiresoptimizations,whichareinherentlyrisky. TOB-BALANCER-003 UseSlither.Slitherwillcatchmanysecurityissueswhilerequiringaloweffort. TOB-BALANCER-004,TOB-BALANCER-005 UseEchidnawhendesigninganewpooltoensurethatswap/join/exitoperations andthepool'sinvariantarerobustagainstroundingissues.Manyarithmeticissues werefoundusingEchidna.TOB-BALANCER-006,TOB-BALANCER-007,TOB-BALANCER-008, TOB-BALANCER-010,TOB-BALANCER-012,TOB-BALANCER-013 UsedifferentiaLfuzzingwhendesigningasystemforwhichanother implementationexists.EchidnacanbeusedasadifferentiaLfuzzertoensurethatthe implementationworksasexpected.TOB-BALANCER-009 Identifyanddocumentallparametersthatcanbechangedbyprivilegedusers. Ensurethatupdates totheseparameterswillhavealimitedimpactonusers' funds. TOB-BALANCER-011 Documenttheabilitiesoftheprivilegedrolesthroughoutthesystem.Thatway, userswillnotbesurprisedwhenothersexercisetheirprivileges.TOB-BALANCER-014

2021hasheyeBalancerV2Assessment|15

FindingsSummary PerBalancer'srequest,thestablepool-relatedfindingsarellocatedattheendofthissection becauseofpossiblefuturedeprecation. #TitleTypeSeverity 1Maliciousmanagercanreinvesttokensto drainthepool Undefined Behavior High 2Transfertozerocanleadtounexpected burns AccessControlsInformational 3Soliditycompileroptimizationscanbe dangerous Undefined Behavior

Informational 4MissingeventsforcriticaloperationsAuditingand Logging Informational
5LackofzerocheckonfunctionsDataValidationLow 10Lackofrobustsafeguardsforpoolswith
anemptytokeninWeightedPool DataValidationHigh 11Protocolfeefront-runDataValidationLow
12Sumofnormalizedweightscanbe differentfrom1 DataValidationLow 14Emergencyperiodtogglingcanbeusedto
selectivelyblocktransactions Undefined Behavior Low 6 StableMath._calcOutGivenIn mayallow freeswaps
DataValidationMedium 7 StableMath._calcInGivenOut mayallow freeswaps DataValidationMedium
8StableMath._calcTokenInGivenExactBpt0 utmayallowanattackerstojoinforfree DataValidationMedium
9BalancerStablePool'sinvariantcandiffer significantlyfromCurve'sinvariant Undefined Behavior
Undetermined 13StablePool'sinvariantisnotmonotonically increasing DataValidationLow
2021hasheyBalancerV2Assessment|16

1.Maliciousmanagercanreinvesttokenstodrainthepool Severity:HighDifficulty:High
Type:UndefinedBehaviorFindingID:TOB-BALANCER-001 Target: PoolRegistry.sol Description
Each token in a pool has a manager who can borrow tokens. A malicious manager could
borrow the tokens, swap them for all the other tokens, and drain the pool. withdrawFromPoolBalance
allows a manager of a token in a pool to withdraw tokens:
function withdrawFromPoolBalance(bytes32 poolId, AssetManagerTransfer[] memory transfers) external
override nonReentrant noEmergencyPeriod { _ensureRegisteredPool(poolId);
PoolSpecializations specialization = _getPoolSpecialization(poolId);
for(uint256 i=0; i<transfers.length; ++i){ IERC20 token=transfers[i].token;
_ensurePoolAssetManagerIsSender(poolId, token); uint256 amount=transfers[i].amount;
if(specialization==PoolSpecialization.MINIMAL_SWAP_INFO){
_minimalSwapInfoPoolCashToManaged(poolId, token, amount);
}elseif(specialization==PoolSpecialization.TWO_TOKEN){
_twoTokenPoolCashToManaged(poolId, token, amount); }elseif
_generalPoolCashToManaged(poolId, token, amount); } token.safeTransfer(msg.sender, amount);
emit PoolBalanceChanged(poolId, msg.sender, token, -(amount.toInt256())); } } Figure 1.1:
vault/PoolRegistry.sol#L512-L537 .

It is expected that a manager can impact or steal only the tokens under his management.
However, as a manager can reinvest the tokens directly and swap them for the other
tokens in the pool, he can drain the pool entirely. Exploit Scenario
Bob deploys a pool with four tokens, one of which Eve manages. Eve withdraws and swaps
all the tokens she is managing for the others, effectively draining the pool.
2021hasheyBalancerV2Assessment|17

Recommendations Short term, take one of the following steps: •
Document the fact that the manager has access to all of the funds in the pool •
Allow one manager per pool, instead of one manager per token
This will prevent user confusion and reduce the risks associated with malicious managers.
Long term, document the expectations for managers and their associated risks. Consider
providing smart contracts that can act as managers with on-chain restrictions.
2021hasheyBalancerV2Assessment|18

2. Transfer to zero can lead to unexpected burns Severity: Informational Difficulty: Low
Type: Access Controls Finding ID: TOB-BALANCER-002 Target: BalancerPoolToken.sol Description
BalancerPoolToken uses a Transfer -to-zero event to indicate a burn. That same event can
be triggered without burning tokens, which could cause confusion among off-chain monitors.
When tokens are burned, the total supply decreases, and a Transfer -to-zero event is emitted:
function _burnPoolTokens(address sender, uint256 amount) internal {
uint256 currentBalance = _balance[sender]; require(currentBalance >= amount, "INSUFFICIENT_BALANCE");
_balance[sender] = currentBalance - amount; _totalSupply = _totalSupply.sub(amount);
emit Transfer(sender, address(0), amount); } Figure 2.1: pools/BalancerPoolToken.sol#L139-L146
Users can emit the same event by calling transfer / transferFrom directly, but the total
supply will not be changed. This divergence can be confusing to off-chain monitors and can
make tracking the system's events more difficult. Recommendations Short term, either create a Burn
event or prevent transfer to the zero address.
Long term, document and test the expected behavior of all of the system's events. Consider using a blockchain-
monitoring system to track any suspicious behavior in the contracts. 2021hasheyBalancerV2Assessment|19

3. Solidity compiler optimizations can be dangerous Severity: Informational Difficulty: Low
Type: Undefined Behavior Finding ID: TOB-BALANCER-003 Target: hardhat.config.ts Description
In BalancerV2, optional compiler optimizations in Solidity are enabled. There have been several optimization-
related bugs in Solidity with security implications,
and optimizations are actively being developed. Solidity compiler optimizations are
disabled by default, and it is unclear how many contracts in the wild actually use them. It is
therefore unclear how well they are being tested and exercised. High-

severity security issues caused by optimization bugs occurred in the past. A high-severity bug in the emscripten-generated solc-js compiler used by Truffle and Remix persisted until late 2018. The fix for this bug was not reported in the Solidity CHANGELOG. Another high-severity optimization bug resulting in incorrect bit shift results was patched in Solidity 0.5.6. More recently, a bug stemming from incorrect caching of keccak256 was reported. A compiler audit of Solidity from November 2018 concluded that the optional optimizations may not be safe. There are likely latent bugs related to optimization and/or new bugs that will be introduced due to future optimizations. Exploit Scenario A latent or future bug in Solidity compiler optimizations or in the Emscripten transpilation to solc-js causes a security vulnerability in the Balancer contracts. Recommendations Short term, measure the gas savings from optimizations, and carefully weigh them against the possibility of an optimization-related bug. Long term, monitor the development and adoption of Solidity compiler optimizations to assess their maturity. 2021hasheyBalancerV2Assessment|20

4. Missing events for critical operations Severity: Informational Difficulty: Low Type: Auditing and Logging Finding ID: TOB-BALANCER-004 Target: pools/BasePool.sol, vault/VaultAuthorization.sol Description Several critical operations do not trigger events, which will make it difficult to check the behavior of the contract once they have been deployed. Ideally, the following critical operations should trigger events: • BasePool.setSwapFee function setSwapFee(uint256 swapFee) external authenticate{ require(swapFee ≤ _MAX_SWAP_FEE, "MAX_SWAP_FEE"); _swapFee = swapFee; } Figure 4.1: pools/BasePool.sol#L181-L184 • VaultAuthorization.changeAuthorizer function changeAuthorizer(IAuthorizer newAuthorizer) external override nonReentrant authenticate{ _authorizer = newAuthorizer; } Figure 4.2: vault/VaultAuthorization.sol#L42-L44 • VaultAuthorization.changeRelayerAllowance function changeRelayerAllowance(address relayer, bool allowed) external override nonReentrant noEmergencyPeriod{ _allowedRelayers[msg.sender][relayer] = allowed; } Figure 4.3: vault/VaultAuthorization.sol#L50-L52 Without events, users and blockchain monitoring systems will not be able to easily detect suspicious behavior. Recommendations Short term, add events for BasePool.setSwapFee, Authorizer.changeAuthorizer, and Authorizer.changeRelayerAllowance. Events will facilitate contract monitoring and the detection of suspicious behavior. 2021hasheyBalancerV2Assessment|21

Long term, add Slither, which found this issue, to your CI. 2021hasheyBalancerV2Assessment|22

5. Lack of zero check on functions Severity: Low Difficulty: High Type: Data Validation Finding ID: TOB-BALANCER-005 Target: pools/BasePoolFactory.sol Description Certain setter functions fail to validate incoming arguments, so callers can accidentally set important state variables to the zero address. These include the constructor in BasePoolFactory, which sets the vault. This contract serves as the base contract for the StablePoolFactory and WeightedPoolFactory contracts. If the vault is set to address zero, subsequent calls to create a StablePool or WeightedPool will revert; to set a correct vault, the pool factory will need to be redeployed. constructor(IVault _vault){ vault = _vault; } Figure 5.3: pools/BasePoolFactory.sol#L26-L28 This issue is also prevalent in the following functions: • AssetTransferHandler.constructor • Authorizer.constructor Exploit Scenario Alice deploys a StablePoolFactory and accidentally sets the vault to address(0). When she invokes the create function to create a StablePool, the transaction reverts because the vault has been set to address(0). Recommendations Short term, add zero-value checks on all function arguments to ensure that users can't accidentally set incorrect values, misconfiguring the system. Long term, use Slither, which will catch functions that do not have zero checks. 2021hasheyBalancerV2Assessment|23

10. Lack of robust safeguards for pools with an empty token in WeightedPool Severity: High Difficulty: High Type: Data Validation Finding ID: TOB-BALANCER-010 Target: WeightedMath.sol, WeightedPool.sol Description The WeightedPool has several corner cases that could either enable a user to receive tokens for free or trap the liquidity if one of the pools has an empty balance. It might not be possible for a user to empty a pool's underlying token balance; however, we recommend adding safeguards to improve the pools' robustness. Cases that could lead to free tokens _calcTokenInGivenExactBptOut determines the number of tokens that a user must send to receive a given number of the tokens in a pool (i.e., single asset deposit): function _calcTokenInGivenExactBptOut(uint256 tokenBalance, uint256 tokenNormalizedWeight, uint256 bptAmountOut, uint256 bptTotalSupply, uint256 swapFee) internal pure returns (uint256){ /***** // tokenInForExactBPTOut // a=tokenAmountIn // b=tokenBalance // totalBPT+bptOut*(1/w) // bptOut=bptAmountOut a=b*|-----|^-1 // bpt=totalBPT\totalBPT*****/

```

//w=tokenWeight//
*****/
//Tokenin,soweroundupoverall.
//CalculatethefactorbywhichtheinvariantwillincreaseaftermintingBPTAmountOut
uint256invariantRatio=bptTotalSupply.add(bptAmountOut).divUp(bptTotalSupply);
//CalculatebyhowmuchthetokenbalancehastoincreasetocauseinvariantRatio
uint256tokenBalanceRatio=FixedPoint.powUp(invariantRatio,
FixedPoint.ONE.divUp(tokenNormalizedWeight));
uint256tokenBalancePercentageExcess=tokenNormalizedWeight.complement();
uint256amountInAfterFee=tokenBalance.mulUp(tokenBalanceRatio.sub(FixedPoint.ONE));
uint256swapFeeExcess=swapFee.mulUp(tokenBalancePercentageExcess);
returnamountInAfterFee.divUp(swapFeeExcess.complement()); 2021hasheyBalancerV2Assessment|24
} Figure10.1: pools/weighted/WeightedMath.sol#L172-L201 Ifthebalanceofthe tokenIn iszero,the
amountIn requiredwillbezero.Anattackermay
beabletoswaptokensforfreeifoneofthetokenshasabalanceofzero.Similarissuescan
occurinotherfunctions,suchas WeightedMath._calcInGivenOut. Casesthatcouldleadtoatrappedpool
Whenauserwantstojoinorexiththepool, _getDueProtocolFeeAmounts iscalled.
uint256[]memorydueProtocolFeeAmounts=_getDueProtocolFeeAmounts( Figure10.1:
pools/weighted/WeightedPool.sol#L266 dueProtocolFeeAmounts=_getDueProtocolFeeAmounts( Figure10.2:
pools/weighted/WeightedPool.sol#L375 _getDueProtocolFeeAmounts dividesby currentInvariant .
uint256invariantRatio=previousInvariant.divUp(currentInvariant); Figure10.3:
pools/weighted/WeightedPool.sol#L500 Ifoneofthebalancesiszero,thepool'sinvariantwillbezero.
function_calculateInvariant(uint256[]memorynormalizedWeights,uint256[]memorybalances) internal pure
returns(uint256invariant) {
/*****/
//invariant____// //wi=weightindexi||wi// //bi=balanceindexi||bi^=i// //i=invariant//
*****/
InputHelpers.ensureInputLengthMatch(normalizedWeights.length,balances.length);
invariant=FixedPoint.ONE; for(uint8i=0;i<normalizedWeights.length;i++){
invariant=invariant.mul(FixedPoint.pow(balances[i],normalizedWeights[i])); } } Figure10.4:
pools/weighted/WeightedMath.sol#L37-L54 2021hasheyBalancerV2Assessment|25

```

Ifoneofthebalancesiszero,thebalancewillbedividedbyzero,causingjoin/exit operationstorevert. Duetothecurrentroundingstrategies,wewerenotabletoemptyapoolthrough swap/exitoperations.However,acoderefactoringoraspecificedgecasemightallowan attackertousetheoperationstoturnaprofit. ExploitScenario Bobdeploysapoolwithfourtokens.Evefindsawaytoemptythepoolofoneofthe tokens,consequentlydrainingitoftheotherthree. Recommendations Shortterm,disallowswap/join/exitoperationsifthe tokenin hasanemptybalanceorif theoperationswouldemptyitout. Longterm,useEchidnawhendesigninganewpooltoensurethattheswap/join/exit operationsarero bustagainstbalance-emptyingattemptsandsimilaredgecases. 2021hasheyBalancerV2Assessment|26

11.Protocolfeefront-run Severity:LowDifficulty:High Type:DataValidationFindingID:TOB-BALANCER-011 Target: PoolRegistry.sol,InternalBalance.sol,ProtocolFeesCollector.sol Description Privilegeduserscanfront-runwithdrawaloperationstoincreasewithdrawalfees, reducing theamountofassetsotheruserswillreceivewhentheyexecutewithdrawals. Withdrawaloperationscarryafee: uint256withdrawFee=toInternalBalance?0:_calculateProtocolWithdrawFeeAmount(amountOut); _sendAsset(assets[i],amountOut.sub(withdrawFee),recipient,toInternalBalance,false); Figure11.1: vault/PoolRegistry.sol#L388-L389 if(taxableAmount>0){ uint256feeAmount=_calculateProtocolWithdrawFeeAmount(taxableAmount); _payFee(token,feeAmount); amountToSend=amountToSend.sub(feeAmount); } _sendAsset(asset,amountToSend,recipient,false,false); Figure11.2: vault/InternalBalance.sol#L99-L105 Thefeeissetthrough setProtocolWithdrawFee : functionsetWithdrawFee(uint256newWithdrawFee)externalauthenticate{ require(newWithdrawFee <= _MAX_PROTOCOL_WITHDRAW_FEE, "WITHDRAW_FEE_TOO_HIGH"); _withdrawFee=newWithdrawFee; emitWithdrawFeeChanged(newWithdrawFee); } Figure11.3: vault/ProtocolFeesCollector.sol#L80-L84 Withdrawaloperationsdonotspecifytheamountofassetsausershouldreceiveafterthe feehasbeenapplied.Asaresult,ifausersendsawithdrawaltransactionandthefeeis updatedbeforethewithdrawalhasbeenminted,theuserwillreceivea lower-than-expectedamountofassets. ExploitScenario Evesetsthefeeto0.Bobwithdrawsassetsworth\$10,000,000.Evefront-runs the withdrawalandsetsthefeeto0.5%.Asaresult,Bobloses\$50,000. Recommendations 2021hasheyBalancerV2Assessment|27

Shortterm, add a minimum withdrawal requirement for withdrawal operations.
Longterm, identify and document all parameters that can be changed by privileged users.
Ensure that updates to these parameters will have a limited impact on users' funds.
2021hasheyeBalancerV2Assessment|28

12. Sum of normalized weights can be different from 1 Severity: Low Difficulty: High
Type: Data Validation Finding ID: TOB-BALANCER-012 Target: WeightedPool.sol Description
The weighted pool token normalizes token weights such that a weight is a percentage of
the tokens' total weight. The computation expects the sum of all weights to be equal to 1,
but rounding may result in a different sum.
To compute normalized weights, the weighted pool constructor sums the weights and
calculates each weight as the weight divided by the sum of the weights:
// Check valid weights and compute normalized weights uint256 sumWeights = 0;
for (uint8 i = 0; i < weights.length; i++) { sumWeights = sumWeights.add(weights[i]); }
uint256 maxWeightTokenIndex = 0; uint256 maxNormalizedWeight = 0;
uint256[] memory normalizedWeights = new uint256[](weights.length);
for (uint8 i = 0; i < normalizedWeights.length; i++) { uint256 normalizedWeight = weights[i].div(sumWeights);
require(normalizedWeight >= _MIN_WEIGHT, "MIN_WEIGHT"); normalizedWeights[i] = normalizedWeight;
if (normalizedWeight > maxNormalizedWeight) { maxWeightTokenIndex = i;
maxNormalizedWeight = normalizedWeight; } }
Figure 12.1: pools/weighted/WeightedPool.sol#L72-L91
Due to the arithmetic precision loss in `weights[i].div(sumWeights)`, the sum of the
normalized weights can be slightly higher or lower than 1. This may break the underlying
assumptions of the pool.
Exploit Scenario Bob deploys a pool with 4 tokens. Their weights are 1, 1, 1, and 3. The sum of the
normalized weights is equal to $10 \times 18 + 1$, which breaks one of the pool's invariants. Recommendations
2021hasheyeBalancerV2Assessment|29

Shortterm, check that the sum of the normalized weights is equal to 10×18 in the
weighted pool's constructor. This will ensure that the pool's invariant is preserved at
deployment.
Longterm, identify the system's invariants, and use Echidna to check their robustness.
2021hasheyeBalancerV2Assessment|30

14. Emergency period toggling can be used to selectively block transactions Severity: Low Difficulty: High
Type: Undefined Behavior Finding ID: TOB-BALANCER-014 Target: EmergencyPeriod.sol Description
The EmergencyPeriod contract allows the admin to repeatedly toggle the emergency
period between active and inactive until the `_emergencyPeriodEndDate` has passed. As
such, a malicious admin could cause transactions of the admin's choosing to fail by
front-running them and then quickly enabling the emergency period.
function _setEmergencyPeriod(bool active) internal {
require(block.timestamp < _emergencyPeriodEndDate, "EMERGENCY_PERIOD_FINISHED");
_emergencyPeriodActive = active; emit EmergencyPeriodChanged(active); }
Figure 14.1: lib/helpers/EmergencyPeriod.sol#L53-L57
function setEmergencyPeriod(bool active) external authenticate {
_setEmergencyPeriod(active); }
Figure 14.2: pools/BasePool.sol#L186-L188
function setEmergencyPeriod(bool active) external authenticate {
_setEmergencyPeriod(active); }
Figure 14.3: vault/Vault.sol#L69-L71
Exploit Scenario
Eve becomes an admin before the emergency period has ended. Eve monitors the
mem pool for transactions executed by Bob. When she finds one, she front-runs the
transaction, quickly enables the emergency period, and then deactivates that period.
Recommendations
Shortterm, document the emergency period-related abilities of an admin so that users will
be well informed.
Longterm, clearly document the abilities of the privileged roles throughout the system.
That way, users will not be surprised when others exercise their privileges.
2021hasheyeBalancerV2Assessment|31

6. StableMath._calcOutGivenIn may allow free swaps Severity: Medium Difficulty: High
Type: Data Validation Finding ID: TOB-BALANCER-006 Target: StableMath.sol Description
The `outGivenIn` function has rounding to calculate swaps, which could enable an attacker
to obtain tokens at no cost.
StableMath._calcOutGivenIn computes the number of tokens that one user will receive
based on the number of tokens sent: `function _calcOutGivenIn(uint256 amplificationParameter,
uint256[] memory balances, uint256 tokenIndexIn, uint256 tokenIndexOut, uint256 tokenAmountIn
) internal pure returns (uint256) {
/*****
// outGivenIn token x for y - polynomial equation to solve // // ay = amount out to calculate //
// by = balance token out // // y = by - ay (finalBalanceOut) // // D = invariant DD^(n+1) //
// A = amplification coefficient y^2 + (S - D) * y - 0 //
// n = number of tokens (A * n^n) * n^2 * P // // S = sum of final balances buty // // P = product of final balances buty //
*****/
// Amount out, so we round down overall.`

```
uint256invariant=_calculateInvariant(amplificationParameter,balances);
balances[tokenIndexIn]=balances[tokenIndexIn].add(tokenAmountIn);
uint256finalBalanceOut=_getTokenBalanceGivenInvariantAndAllOtherBalances( amplificationParameter,
balances, invariant, tokenIndexOut );
balances[tokenIndexIn]=balances[tokenIndexIn].sub(tokenAmountIn);
2021hasheyeBalancerV2Assessment|32
```

returnbalances[tokenIndexOut].sub(finalBalanceOut).sub(1); } Figure6.1:
pools/stable/StableMath.sol#L89-L124 _calcOutGivenIn performs: $0000000000 = 00000000000000000000(000, 00000000) 00000000[00000000] = 00000000[00000000] + 00000000000000 00000000000000 = 0000000000000000$
[.]00000000(000, 00000000, 000000000000, 0000000000) _calculateInvariant and
_getTokenBalanceGivenInvariantAndAllOtherBalances

containoperationsthatcanroundupordownaccordingtotheirvalues. Forexample,
_getTokenBalanceGivenInvariantAndAllOtherBalances uses FixedPoint.mul
,whichcanroundupordownbasedonthevalue: tokenBalance=tokenBalance.mul(tokenBalance) .add(c) .divUp(
Math.mul(tokenBalance,2) .add(b) .sub(invariant)); Figure6.2: pools/stable/StableMath.sol#L489

Asaresult, _calcOutGivenIn canroundinadirectionthatalloswsanattacker toreceive
freetokensbyeitherswappingwith0 tokenin forasmallamountof tokenout or
accumulatingdustthroughcallsto StableMath._calcOutGivenIn.
Weclassifiedthisissueasoneofmediumseverity,aswewerenotabletogeneratedfree
tokenswithlargebalances.However,thatmightstillbepossibleincertainedgecases. ExploitScenario • Ampis
4168774334271564283904 . • Thepoolhas4tokens,andthebalancesare 35303029 , 1524785991 , 323536 ,and
323534 . • Eveswaps62,439,391ofthetokensinindex1for0tokensinindex0. Recommendations ShortTerm •
Remove FixedPoint.mul and FixedPoint.div ,andensurethateveryfunctionuses
theappropriateroundingdirection. • Createtwoversionsof _calculateInvariant and
_getTokenBalanceGivenInvariantAndAllOtherBalances thatroundupordown,
respectively,andusethemappropriately. 2021hasheyeBalancerV2Assessment|33

Longterm,useEchidnawhendesigninganewpooltoensurethattheswap/join/exit
operationsarerojustagainstroundingissues. 2021hasheyeBalancerV2Assessment|34

7.StableMath._calcInGivenOutmayallowfreeswaps Severity:MediumDifficulty:High
Type:DataValidationFindingID:TOB-BALANCER-007 Target: StableMath.sol Description Thein-given-
outfunctionhasroundingtocalculateswaps,whichcouldenableanattacker toobtaintokensatnocost.

StableMath._calcOutGivenOut computesthenumberoftokensthatoneuserwillreceive
basedonthenumberoftokensent: function_calcInGivenOut(uint256amplificationParameter,
uint256[]memorybalances, uint256tokenIndexIn, uint256tokenIndexOut, uint256tokenAmountOut
)internalpurereturns(uint256){
/*****
//inGivenOuttokenxfory-polynomialequationtosolve// //ax=amountintocalculate// //bx=balancetokenin//
//x=bx+ax(finalBalanceIn)// //D=invariantDD^(n+1)// //A=amplificationcoefficientx^2+(S-----
D)*x-----=0// //n=numberoftokens(A*n^n)A*n^2n*P// //S=sumoffinalbalancesbutx//
//P=productoffinalbalancesbutx//
*****/
//Amountin,soweroundupoverall.

```
uint256invariant=_calculateInvariant(amplificationParameter,balances);
balances[tokenIndexOut]=balances[tokenIndexOut].sub(tokenAmountOut);
uint256finalBalanceIn=_getTokenBalanceGivenInvariantAndAllOtherBalances( amplificationParameter,
balances, invariant, tokenIndexIn );
balances[tokenIndexOut]=balances[tokenIndexOut].add(tokenAmountOut);
2021hasheyeBalancerV2Assessment|35
```

returnfinalBalanceIn.sub(balances[tokenIndexIn]).add(1); } Figure7.1:
pools/stable/StableMath.sol#L129-L164 _calcOutGivenOut performs: $0000000000 = 00000000000000000000(000,$
 $00000000) 00000000[00000000] = 00000000[00000000] - 00000000000000 00000000000000 = 0000000000000000$
[.]00000000(000, 00000000, 000000000000, 0000000000) _calculateInvariant and
_getTokenBalanceGivenInvariantAndAllOtherBalances

containoperationsthatcanroundupordownaccordingtotheirvalues. Forexample,
_getTokenBalanceGivenInvariantAndAllOtherBalances uses FixedPoint.mul
,whichcanroundupordownbasedonthevalue: tokenBalance=tokenBalance.mul(tokenBalance) .add(c) .divUp(
Math.mul(tokenBalance,2) .add(b) .sub(invariant)); Figure7.2: pools/stable/StableMath.sol#L489

Asaresult, _calcOutGivenOut canroundinadirectionthatalloswsanattacker toreceive
freetokensbyaccumulatingdustwithcallsto StableMath._calcOutGivenOut .
Weclassifiedthisissueasoneofmediumseverity,aswewerenotabletogeneratedfree
tokenswithlargebalances.However,thatmightstillbepossibleincertainedgecases. ExploitScenario •
Ampis10**18. • Thebalancesare20,369,17,465,037,809,and1. •

Deswaps1wei of the tokens in index 0 and receives 37,808 wei of the tokens in index 2. • Eve then swaps 37,808 wei of the tokens in index 2 and receives 20,369 wei of the tokens in index 0. • As a result, Eve receives 20,368 wei of the tokens in index 0 for free. Recommendations ShortTerm • Remove FixedPoint.mul and FixedPoint.div, and ensure that every function uses the appropriate rounding direction. 2021hasheyeBalancerV2Assessment|36

• Create two versions of _calculateInvariant and _getTokenBalanceGivenInvariantAndAllOtherBalances that round up or down, respectively, and use them appropriately. Long term, use Echidna when designing a new pool to ensure that the swap/join/exit operations are robust against rounding issues. 2021hasheyeBalancerV2Assessment|37

8. StableMath._calcTokenInGivenExactBptOut may allow an attacker to join for free Severity: Medium Difficulty: High Type: Data Validation Finding ID: TOB-BALANCER-008 Target: StableMath.sol Description The "join" operation for token-in-for-exact-bpt-out has rounding, which could allow an attacker to join a pool without paying any tokens. StableMath._calcTokenInGivenExactBptOut determines the number of tokens that a user must send to receive a given number of BPT tokens (for a single asset): function _calcTokenInGivenExactBptOut(uint256 amp, uint256[] memory balances, uint256 tokenIndex, uint256 bptAmountOut, uint256 bptTotalSupply, uint256 swapFee) internal pure returns (uint256) { // Token in, so we round up overall. // Get current invariant uint256 currentInvariant = _calculateInvariant(amp, balances); // Calculate new invariant uint256 newInvariant = bptTotalSupply.add(bptAmountOut).divUp(bptTotalSupply).mulUp(currentInvariant); // First calculate the sum of all token balances which will be used to calculate // the current weight of token uint256 sumBalances = 0; for (uint256 i = 0; i < balances.length; i++) { sumBalances = sumBalances.add(balances[i]); } // Get amount in after fee uint256 newBalanceTokenIndex = _getTokenBalanceGivenInvariantAndAllOtherBalances(amp, balances, newInvariant, tokenIndex); uint256 amountInAfterFee = newBalanceTokenIndex.sub(balances[tokenIndex]); 2021hasheyeBalancerV2Assessment|38

// Get token balance percentage excess uint256 currentWeight = balances[tokenIndex].divDown(sumBalances); uint256 tokenBalancePercentageExcess = currentWeight.complement(); uint256 swapFeeExcess = swapFee.mulUp(tokenBalancePercentageExcess); return amountInAfterFee.divUp(swapFeeExcess.complement()); } Figure 8.1: pools/stable/StableMath.sol#L129-L164 _calcTokenInGivenExactBptOut performs: $00000000000000000000 = 00000000000000000000(000, 00000000) 000000000000 = 0000000000000000 + 000000000000 000000000000 0 * 0 000000000000 000000000000 = 0 \sum 00000000[0] 00000000000000000000 = 00000000000000[.]00000000(000, 0000000, 00000000000, 000000000) _calculateInvariant and _getTokenBalanceGivenInvariantAndAllOtherBalances contain operations that can round up or down according to their values. For example, _getTokenBalanceGivenInvariantAndAllOtherBalances uses FixedPoint.mul, which can round up or down based on the value. tokenBalance = tokenBalance.mul(tokenBalance).add(c).divUp(Math.mul(tokenBalance, 2).add(b).sub(invariant)); Figure 8.2: pools/stable/StableMath.sol#L489 As a result, _calcTokenInGivenExactBptOut can round in a direction that allows an attacker to receive BPT tokens without paying any tokens.$

We classified this issue as one of medium severity, as we were not able to generate free tokens with large balances. However, that might still be possible in certain edge cases. Exploit Scenario • Ampis 287584007913129639935. • There are 4 tokens in the pool, each of which has a balance of 100,000,000,000,000,000. • The current BPT supply is 5,690,710,977,914,755,780,762,205. 2021hasheyeBalancerV2Assessment|39

• Eve joins the pool to obtain 1,000,021 BPT tokens without having to make a payment. Recommendations ShortTerm • Remove FixedPoint.mul and FixedPoint.div, and ensure that every function uses the appropriate rounding direction • Create two versions of _calculateInvariant and _getTokenBalanceGivenInvariantAndAllOtherBalances that round up or down, respectively, and use them appropriately. Long term, use Echidna when designing a new pool to ensure that the swap/join/exit operations are robust against rounding issues. 2021hasheyeBalancerV2Assessment|40

9. BalancerStablePool's invariant can differ significantly from Curve's invariant Severity: Undetermined Difficulty: Medium Type: Undefined Behavior Finding ID: TOB-BALANCER-009 Target: StableMath.sol Description Balancer implements StablePool with a formula based on Curve's formula. The two implementations employ different orders of operations and rounding strategies, leading to different results. The impact of this difference is unclear and requires further investigation. Curve's invariant is as follows: def get_D(xp: uint256[N_COINS], amp: uint256) → uint256: "" D invariant calculation in non-overflowing integer operations iteratively $A * \sum(x_i)^{n+1} + D = A * D * n^{n+1} + D * (n+1) / (n * \prod(x_i))$ Converging solution: $D[j+1] = (A * n * \sum(x_i) - D[j] * (n+1) / (n * \prod(x_i))) / (A * n - 1)$ "" S: uint256 = 0 for_x in xp: S += x if S == 0: return 0 Dprev: uint256 = 0 D: uint256 = S Ann: uint256 = amp * N_COINS for_i in range(255): D_P: uint256 = D for_x in xp:

```
D_P=D_P*D/(x*N_COINS+1)#+1istopprevent/0 Dprev=D D=(Ann*S/A_PRECISION+D_P*N_COINS)*D/((Ann-
A_PRECISION)*D/ A_PRECISION+(N_COINS+1)*D_P) #Equalitywiththeprecisionof1 ifD>Dprev: ifD-Dprev≤1:
returnD else: ifDprev-D≤1: returnD
#convergence typically occurs in 4 rounds or less, this should be unreachably!
2021hasheyeBalancerV2Assessment|41
```

```
#ifitdoeshappenthepoolisborkedandLPscanwithdrawvia`remove_liquidity` raise
Figure9.1:Curve'sinvariant Balancer'sinvariantisasfollows:
function_calculateInvariant(uint256amplificationParameter,uint256[]memorybalances) internal pure
returns(uint256) {
/***** //invariant//
//D=invariantD^(n+1)// //A=amplificationcoefficientAn^nS+D=ADn^n+----- //
//S=sumofbalances^nP// //P=productofbalances// //n=numberoftokens//
*****/
//Weroundupinvariant. uint256sum=0; uint256numTokens=balances.length;
for(uint256i=0;i<numTokens;i++){ sum=sum.add(balances[i]); } if(sum==0){ return0; }
uint256prevInvariant=0; uint256invariant=sum;
uint256ampTimesTotal=Math.mul(amplificationParameter,numTokens); for(uint256i=0;i<255;i++){
uint256P_D=Math.mul(numTokens,balances[0]); for(uint256j=1;j<numTokens;j++){
P_D=Math.divUp(Math.mul(Math.mul(P_D,balances[j]),numTokens),invariant); } prevInvariant=invariant;
invariant=Math.divUp( Math.mul(Math.mul(numTokens,invariant),
invariant).add(Math.mul(Math.mul(ampTimesTotal,sum),P_D)),
Math.mul(numTokens.add(1),invariant).add(Math.mul(ampTimesTotal.sub(1),P_D)) );
if(invariant>prevInvariant){ if(invariant.sub(prevInvariant)≤1){
2021hasheyeBalancerV2Assessment|42
```

```
break; } }elseif(prevInvariant.sub(invariant)≤1){ break; } } returninvariant; }
Figure9.2:Balancer'sinvariant, pools/stable/StableMath.sol#L36-L84
WhileCurveandBalancerusethe same formula, they used different orders of operations
and rounding methods. Additionally, Curve reverts if the precision loop does not converge
after 255 iterations, while Balancer returns the value, potentially with a significant loss of precision.
We implemented a differential fuzzer through Echidna (described in Appendix 6), which
showed that the implementations can return significantly different values. For example,
with 4 tokens with balances of 1;1;54,066;and 108,075,532 and an amplitude of
83,437,555, Curve returns 964,800, while Balancer returns 101,906,431, leading to a
difference in magnitude of 10**8.
This difference merits further consideration, as it is unclear whether it could lead to
unexpected arbitrage or other issues. Exploit Scenario
Eve exploits unexpected arbitrage opportunities between Balancer and Curve, generating a
profit. Bob notices the operation and loses confidence in Balancer's arithmetic. Recommendations
Short term, investigate the differences between the Balancer and Curve invariants, and
evaluate their impact on arbitrage opportunities and potential associated risks.
Long term, use differential fuzzing when designing a system for which another implementation exists.
2021hasheyeBalancerV2Assessment|43
```

```
13. StablePool'sinvariant is not monotonically increasing Severity:Low Difficulty:High
Type:Data Validation Finding ID:TOB-BALANCER-013 Target: StableMath.sol Description
StableMath._calculateInvariant returns the pool's invariant, which indicates the value
of the pool. The invariant is expected to be monotonically increasing but is not. StableMath._calculateInvariant
returns the pool's invariant and is an approximation of the following: Figure 13.1: The pool's invariant
function_calculateInvariant(uint256amplificationParameter,uint256[]memorybalances) internal pure
returns(uint256) {
/***** //invariant//
//D=invariantD^(n+1)// //A=amplificationcoefficientAn^nS+D=ADn^n+----- //
//S=sumofbalances^nP// //P=productofbalances// //n=numberoftokens//
*****/
//Weroundupinvariant. uint256sum=0; uint256numTokens=balances.length;
for(uint256i=0;i<numTokens;i++){ sum=sum.add(balances[i]); } if(sum==0){ return0; }
2021hasheyeBalancerV2Assessment|44
```

```
uint256prevInvariant=0; uint256invariant=sum;
uint256ampTimesTotal=Math.mul(amplificationParameter,numTokens); for(uint256i=0;i<255;i++){
uint256P_D=Math.mul(numTokens,balances[0]); for(uint256j=1;j<numTokens;j++){
P_D=Math.divUp(Math.mul(Math.mul(P_D,balances[j]),numTokens),invariant); } prevInvariant=invariant;
invariant=Math.divUp( Math.mul(Math.mul(numTokens,invariant),
invariant).add(Math.mul(Math.mul(ampTimesTotal,sum),P_D)),
```

```
Math.mul(numTokens.add(1), invariant).add(Math.mul(ampTimesTotal.sub(1), P_D)) );
if(invariant>prevInvariant){ if(invariant.sub(prevInvariant)≤1){ break; }
}elseif(prevInvariant.sub(invariant)≤1){ break; } } returninvariant; } Figure13.2:
```

pools/stable/StableMath.sol#L36-L84

Thisinvariantisexpectedtoincreaseifthebalanceofthepoolincreases.Duetothe incorrectapplicationof
_calculateInvariant ,thisassumptioncanbeproken.Asareult, thepool'sinvariantcoulddecreaseovertime.

ExploitScenario Bobdeploysastablepoolwith4tokens.Theirbalancesare1;2;

17,464,062,808,818,790,875;and14,953,662,333,476,747,andthe amp parameteris

1,001,313,087,410,729,399.

Thecurrentinvariantis6,600,767,538,511,083,210.Thebalanceofeachtokenincreasesby

1wei.Thepoolinvariantisnow6,600,767,538,511,083,209(i.e.,theoriginalinvariant,less

1).Asareult,thepoolhaslostvalue,whilethebalancehasincreased. Recommendations

Shortterm,applythecorrectroundingin StableMath._calculateInvariant.

Longterm,identifythesystem'sinvariants,anduseEchidnatochecktheirrobustness.

2021hasheyBalancerV2Assessment|45

A.VulnerabilityClassifications VulnerabilityClasses ClassDescription

AccessControlsRelatedtoauthorizationofusersandassessmentofrights

AuditingandLoggingRelatedtoauditingofactionsorloggingofproblems

AuthenticationRelatedtotheidentificationofusers

ConfigurationRelatedtosecurityconfigurationsofservers,devices,or software

CryptographyRelatedtoprotectingtheprivacyorintegrityofdata

DataExposureRelatedtounintendedexposureofsensitiveinformation

DataValidationRelatedtoimproperrelianceonthestructureorvaluesofdata

DenialofServiceRelatedtocausingasystemfailure

ErrorReportingRelatedtothereportingoferrorconditionsinasecurefashion

PatchingRelatedtokeepingsoftwareuptodate

SessionManagementRelatedtotheidentificationofauthenticatedusers

TimingRelatedtoraceconditions,locking,ortheorderofoperations

UndefinedBehaviorRelatedtoundefinedbehaviortriggeredbytheprogram SeverityCategories

SeverityDescription InformationalTheissuedoesnotposeanimmateriskbutisrelevanttosecurity

bestpracticesorDefenseinDepth. UndeterminedTheextentoftheriskwasnotdeterminedduringthisengagement.

LowTheriskisrelativelysmallorisnotariskthecustomerhasindicatedis important.

MediumIndividualusers'informationisatrisk;exploitationcouldpose 2021hasheyBalancerV2Assessment|46

reputational,legal,ormoderatefinancialriskstotheclient.

HighTheissuecouldaffectnumeroususersandhaveseriousreputational,

legal,orfinancialimplicationsfortheclient. DifficultyLevels DifficultyDescription

UndeterminedThedifficultyofexploitationwasnotdeterminedduringthis engagement.

LowCommonlyexploitedpublictoolsexist,orsuchtoolscanbescripted.

MediumAnattackermustwriteanexploitorwillneedin-depthknowledgeofa complexsystem.

HighAnattackermusthaveprivilegedinsideraccesstothesystem,may

needtoknowextremelycomplexttechnicaldetails,ormustdiscover otherweaknessestoexploitthisissue.

2021hasheyBalancerV2Assessment|47

B.CodeMaturityClassifications CodeMaturityClasses CategoryNameDescription

AccessControlsRelatedtotheauthenticationandauthorizationofcomponents

ArithmeticRelatedtotheproperuseofmathematicaloperationsand semantics

AssemblyUseRelatedtotheuseofinlineassembly

CentralizationRelatedtotheexistenceofasinglepointoffailure

CodeStabilityRelatedtotherecentfrequencyofcodeupdates UpgradeabilityRelatedtocontractupgradeability

Function Composition Relatedtoseparationofthelogicintofunctionswithclearpurposes Front-

RunningRelatedtoresilienceagainstfront-running

KeyManagementRelatedtotheexistenceofproperproceduresforkeygeneration, distribution,andaccess

MonitoringRelatedtotheuseofeventsandmonitoringprocedures

SpecificationRelatedtotheexpectedcodebaseddocumentation Testing& Verification

Relatedtotheuseoftestingtechniques(unittests,fuzzing,symbolic execution,etc.) RatingCriteria

RatingDescription StrongThecomponentwasreviewed,andnoconcernswerefound.

SatisfactoryThecomponenthadonlyminorissues. ModerateThecomponenthadsomeissues.

WeakThecomponentledtomultipleissues;moreissuesmightbepresent. 2021hasheyBalancerV2Assessment|48

MissingThecomponentwasmising. NotApplicableThecomponentisnotapplicable.

NotConsideredThecomponentwasnotreviewed. Further Investigation Required

Thecomponentrequiresfurtherinvestigation. 2021hasheyBalancerV2Assessment|49

C.CodeQualityRecommendations

Thefollowingrecommendationsarenotassociatedwithspecificvulnerabilities.However,

ability and may prevent the introduction of vulnerabilities in the future. PoolRegistry •
Remove the counter library. The library is used only twice, once to read its value
and once to increment it. Using a library for these purposes is cumbersome. BasePool •
Remove BasePoolAuthorization from the BasePool's constructor. There is no constructor for
BasePoolAuthorization (or Authentication), but users may
incorrectly assume that calling it will result in initialization. •
Consider emitting an event with the registered pool parameters in the constructor. This will make it easy for off-
chain systems to monitor the creation of new pools. BasePoolFactory •
Remove unused import IBasePool. The contract does not use this interface. StablePoolUserDataHelpers •
Rename minBPTAmountIn as minBPTAmountOut in exactTokensInForBptOut. The ABI-
decoded arguments signifies BPTOut, not in. WeightedPoolUserDataHelpers •
Rename minBPTAmountIn as minBPTAmountOut in exactTokensInForBptOut. The ABI-
decoded arguments signifies BPTOut, not in. CodeSize Optimizations
The contracts are approaching the code size limit. We recommend making the following
changes to reduce the contracts' code size: •
Replace modifiers with internal calls. The compiler generates boilerplate code for
modifiers that is not optimized and leads to code duplication. Replacing modifiers
with internal calls will reduce the code size in some cases (see #6584). 2021hasheyeBalancerV2Assessment|50

- Remove trackExempt from AssetTransfersHandler._sendAsset. The parameter is false
in all of the calls (aside from those in the mock contracts) and can be removed. • Remove the bit mask from
PoolRegistry._getPoolAddress. The bit wise shifting
to the right already ensures that the leading bits are zero. Moreover, the value is
cast to an address that applies the same mask. 2021hasheyeBalancerV2Assessment|51

D. Token Integration Checklist

The following checklist provides recommendations for interactions with arbitrary tokens.
Every unchecked item should be justified, and its associated risks, understood. An up-to-
date version of the checklist can be found in [cryptic/building-secure-contracts](#).
For convenience, all Slither utilities can be run directly on a token address, such as the following: `slither-check-erc0xdac17f958d2ee523a2206206994597c13d831ec7TetherToken`
To follow this checklist, use the below output from Slither for the token: `-slither-check-erc[contractName][optional:--ercERC_NUMBER] -slither[contractName]--print-human-summary -slither[contractName]--print-contract-summary -slither-prop.--contractContractName#requires configuration, and use of Echidna and Manticore` General Security Considerations ☐
The contract has a security review. Avoid interacting with contracts that lack a
security review. Check the length of the assessment (i.e., the level of effort), the
reputation of the security firm, and the number and severity of the findings. ☐
You have contacted the developers. You may need to alert their team to an
incident. Look for appropriate contacts on [blockchain-security-contacts](#). ☐
They have a security mailing list for critical announcements. Their team should
advise users (like you!) when critical issues are found or when upgrades occur. ERC Conformity
Slither includes a utility, `slither-check-erc`, that reviews the conformance of a token to
many related ERC standards. Use `slither-check-erc` to review the following: ☐ `Transfer` and `transferFrom`
`return` boolean. Several tokens do not return a
boolean on these functions. As a result, their calls in the contract might fail. ☐ `TheName`, `decimals`, and
`symbol` functions are present if used. These functions are optional in the ERC20 standard and may not be present. ☐
`Decimals` returns a `uint8`. Several tokens incorrectly return a `uint256`. In such
2021hasheyeBalancerV2Assessment|52

cases, ensure that the value returned is below 255. ☐
The token mitigates the known ERC20 race condition. The ERC20 standard has a
known ERC20 race condition that must be mitigated to prevent attackers from stealing tokens. ☐
The token is not an ERC777 token and has no external function call in `transfer` and `transferFrom`.
External calls in the transfer functions can lead to reentrancies. Slither includes a utility, `slither-prop`,
that generates unit tests and security properties that can discover many common ERC flaws. Use `slither-prop`
to review the following: ☐ The contract passes all unit tests and security properties from `slither-prop`.
Run the generated unit tests and then check the properties with Echidna and Manticore.
Finally, there are certain characteristics that are difficult to identify automatically. Conduct
a manual review of the following conditions: ☐ `Transfer` and `transferFrom`
should not take a fee. Deflationary tokens can lead to unexpected behavior. ☐
Potential interest earned from the token is taken into account. Some tokens
distribute interest to token holders. This interest may be trapped in the contract if not taken into account.
Contract Composition ☐ The contract avoids unnecessary complexity. The token should be a simple
contract; a token with complex code requires a higher standard of review. Use Slither's `human-summary`
printer to identify complex code. ☐ The contract uses `SafeMath`. Contracts that do not use `SafeMath`

require a higher standard of review. Inspect contract by hand for SafeMath usage.
The contract has only a few non-token-related functions. Non-token-related functions increase the likelihood of an issue in the contract. Use Slither's contract-summary printertobroadly review the code used in the contract.
The token has only one address. Tokens with multiple entry points for balance updates can break internal bookkeeping based on the address (e.g., balances[token_address][msg.sender] may not reflect the actual balance). Owner Privileges
The token is not upgradeable. Upgradeable contracts may change their rules over time. Use Slither's human-summary printertodetermine if the contract is upgradeable. 2021hasheyBalancerV2Assessment|53

The owner has limited minting capabilities. Malicious or compromised owners can abuse minting capabilities. Use Slither's human-summary printertoreview minting capabilities, and consider manually reviewing the code.
The token is not pausable. Malicious or compromised owners can trap contracts relying on pausable tokens. Identify pausable code by hand.
The owner cannot blacklist the contract. Malicious or compromised owners can trap contracts relying on tokens with a blacklist. Identify blacklisting features by hand.
The team behind the token is known and can be held responsible for abuse. Contracts with an anonymous development team or team that resides in legal shelters require a higher standard of review. Token Scarcity
Reviews of token scarcity issues must be executed manually. Check for the following conditions:
The supply is owned by more than a few users. If a few users own most of the tokens, they can influence operations based on the tokens' repartition.
The total supply is sufficient. Tokens with a low total supply can be easily manipulated.
The tokens are located in more than a few exchanges. If all the tokens are in one exchange, a compromise of the exchange could compromise the contract relying on the token.
Users understand the risks associated with a large amount of funds or flash loans. Contracts relying on the token balance must account for attackers with a large amount of funds or attack executed through flash loans.
The token does not allow flash minting. Flash minting can lead to substantial swings in the balance and the total supply, which necessitate strict and comprehensive overflow checks in the operation of the token. 2021hasheyBalancerV2Assessment|54

E. Risks Associated with Arbitrary Pools

Balancer aims to accept arbitrary pools, the code of which has not been vetted by developers. Arbitrary pools introduce additional issues that could allow an attacker to steal users' funds. We recommend that users review the pool code to ensure it behaves as expected. Pools should meet the following criteria:
• They should not be upgradeable. Upgradeable pools have inherited risks.
• They should be unable to self-destruct. Destructible pools have inherited risks; for example, they may be subject to malicious upgrades through create2.
• Pools should have a clear fee schema and should not allow users to steal funds using high fees. Users must be aware of the amount of fees that pools earn on and take from transactions.
• Pools should not have a call to deregisterTokens. If a pool can call deregisterTokens, it may be able to trap users' funds.
• Pool tokens' weight should be immutable and bounded. Otherwise, an attacker could abuse updates to a token's weight to gain a profit.
• Tokens with decimals $\neq 18$ should be handled correctly. Tokens with different decimals can lead to incorrect price computations.
• Pools should have documented parameters. Each pool's parameters must be documented and made clear to users.
• Pools should favor immutable parameters. Immutable parameters reduce the risks associated with privileged users. 2021hasheyBalancerV2Assessment|55

F. Checking Non-Reentrant Modifiers with Slither

The Balancer code base has many functions that can interact with third-party pools. As a result, most of the functions are protected by a non-reentrant modifier. We used Slither to identify and review the functions that are not protected by a modifier.
The following script uses a whitelist approach, in which every reachable function must be either protected with a non-reentrant modifier or whitelisted. No issues were found using the script.
from slither import Slither
from slither.core.declarations import Contract
from typing import List
contracts = Slither(".", ignore_compile=True)
def check_access_controls(
 contract: Contract,
 modifiers_access_controls: List[str],
 whitelist: List[str]):
 print(f"### Check {contract} access controls")
 no_bug_found = True
 for function in contract.functions_entry_points:
 if function.is_constructor:
 continue
 if function.view:
 continue
 if not function.modifiers or (
 not any((str(x) in modifiers_access_controls) for x in function.modifiers)):
 if not function.name in whitelist:
 print(f"\t-{function.canonical_name} should have a non-reentrant modifier")
 no_bug_found = False
 if no_bug_found:
 print("\t-No bug found")
 _check_access_controls(

```
contracts.get_contract_from_name("Vault"), ["nonReentrant"],
["queryBatchSwap", "receive", "setEmergencyPeriod"],) 2021hasheyeBalancerV2Assessment|56
```

G. Differential Fuzzing on Balancer <Curve

The Balancer codebase implements a stable pool with a formula based on Curve's formulas. Using Echidna, we developed a differential fuzzer to fuzz test the two implementations. The differential fuzzer runs both the Curve and Balancer invariant functions and looks for cases in which the functions return values with a difference of at least 10^{**8} . We discovered issue TOB-BALANCER-09 using the differential fuzzer.

```
import "./StableMath.sol";
interface Curve {
    function get_D(uint256[4] memory, uint256) external view returns (uint256);
}
contract DifferentialFuzzing is StableMath {
    using FixedPoint for uint256;
    uint256 internal constant A_PRECISION = 100; // Curve amplification precision
    Curve c;
    constructor() public {
        address curve_addr;
        bytes memory curve_bytecode =
            hex"61033056600436101561000d57610326565b600035601c52600051341561002157600080fd5b63c763592c81
            14156103245760006101405261018060006004818352015b60206101805102600401356101605261014080516101
            6051818183011101561006657600080fd5b808201905090508152505b815160010180835281141561003f575b5050
            61014051151561009857600060005260206000f35b60006101605261014051610180526084356004808202821582
            84830414176100bf57600080fd5b809050905090506101a0526101c0600060ff818352015b610180516101e05261
            022060006004818352015b6020610220510260040135610200526101e05161018051808202821582848304141761
            011557600080fd5b80905090509050610200516004808202821582848304141761013657600080fd5b8090509050
            90506001818183011101561014e57600080fd5b80820190509050808061016057600080fd5b8204905090506101e0
            525b81516001018083528114156100ea575b505061018051610160526101a0516101405180820282158284830414
            176101a157600080fd5b809050905090506064808204905090506101e051600480820282158284830414176101cb
            57600080fd5b8090509050905081818301110156101e157600080fd5b808201905090506101805180820282158284
            8304141761020057600080fd5b809050905090506101a05160648082101561021a57600080fd5b80820390509050
            61018051808202821582848304141761023957600080fd5b8090509050905060648082049050905060056101e051
            808202821582848304141761026357600080fd5b80905090509050818183011101561027957600080fd5b80820190
            509050808061028b57600080fd5b82049050905061018052610160516101805111156102da576001610180516101
            6051808210156102ba57600080fd5b808203905090501115156102d5576101805160005260206000f35b61030c56
            5b60016101605161018051808210156102f157600080fd5b8082039050905011151561030c576101805160005260
            2021hasheyeBalancerV2Assessment|57
```

```
206000f35b81516001018083528114156100d6575b505060006000fd5b505b60006000fd5b610004610330036100
04600039610004610330036000f3";
uint size = curve_bytecode.length;
assembly {
    curve_addr := create(0, 0xa0, size)
}
c = Curve(curve_addr);
uint limit = 10**8;
function test(uint[4] memory balances, uint amp) public {
    uint curve_value = c.get_D(balances, amp * A_PRECISION);
    uint[] memory balances_dynamic_array = new uint[](4);
    balances_dynamic_array[0] = balances[1];
    balances_dynamic_array[1] = balances[1];
    balances_dynamic_array[2] = balances[2];
    balances_dynamic_array[3] = balances[3];
    uint balance_value = calculateInvariant(amp, balances_dynamic_array);
    if (curve_value > balance_value) {
        assert(curve_value - balance_value < limit);
    }
    if (curve_value < balance_value) {
        assert(balance_value - curve_value < limit);
    }
}
}
Figure 6: Echidna-based differential fuzzer.
2021hasheyeBalancerV2Assessment|58
```

H. Fixed-Point Rounding Recommendations The Balancer codebase uses fixed-point arithmetic. Our initial recommendations regarding the rounding strategies to apply to the WeightedPool are included below. We recommended applying a strategy of rounding down or up such that the operations are always beneficial to the pool.

The process of determining the rounding direction for each operation is described below. Rounding Primitives The mul and div operations are arithmetic primitives of the fixed point: $\frac{a}{b} \cdot \frac{c}{d} = \frac{a * c}{b * d} + 10^{**18} 2$

```
function mul(uint256 a, uint256 b) internal pure returns (uint256) {
    uint256 c0 = a * b;
    require(a == 0 || c0 / a == b, "ERR_MUL_OVERFLOW");
    uint256 c1 = c0 + (ONE / 2);
    require(c1 >= c0, "ERR_MUL_OVERFLOW");
    uint256 c2 = c1 / ONE;
    return c2;
}
Figure F.1: math/FixedPoint.sol#L82-L89
 $\frac{a}{b} \cdot 10^{**18} + \frac{a}{b} 2$ 
function div(uint256 a, uint256 b) internal pure returns (uint256) {
    require(b != 0, "ERR_DIV_ZERO");
    uint256 c0 = a * ONE;
    require(a == 0 || c0 / a == ONE, "ERR_DIV_INTERNAL");
    // mul overflow
    uint256 c1 = c0 + (b / 2);
    require(c1 >= c0, "ERR_DIV_INTERNAL");
    // add
    require(uint256 c2 = c1 / b;
    return c2;
}
Figure F.2: math/FixedPoint.sol#L100-L108
```

Every arithmetic operation (for both swaps and liquidity) is based on these primitives.

2021hasheyeBalancerV2Assessment|59

Fixed-Point Primitives In non-fixed-point arithmetic, multiplication does not lose precision (if we ignore overflow). Only division operations need the two primitives to approximate results. Rounding down is the default behavior: $\frac{a}{b} \cdot \frac{c}{d} = \frac{a * c}{b * d}$ The below approximation can be used to round up a division operation. (See Number Conversion, Roland Backhouse.) $\frac{a}{b} \cdot \frac{c}{d} = \frac{a * c}{b * d} + 1$

